

# INTELLIGENT CONTROL FOR ELECTRO-HYDRAULIC PROPORTIONAL POSITION SERVO SYSTEM<sup>①</sup>

Luo An, Gui Weihua

*Department of Automatic Control Engineering,  
Central South University of Technology, Changsha 410083*

**ABSTRACT** The structure and performance of the electrohydraulic proportional position servo system (EHPPS) were discussed. The intelligent pole placement position control strategy was presented, and its existence was proved. Besides, according to the characteristic of the flow discontinuity for symmetric valve controlling unsymmetric cylinder, a method of digital flow compensation was given. Simulations and experiments showed that the system has good control performance and robustness.

**Key word** intelligent control pole placement digital flow compensation electrohydraulic proportional control

## 1 INTRODUCTION

Although many feedback control system can be satisfactorily controlled by conventional control means, it is often difficult to satisfy the demand of control performance when the parameters of the controlled system exist time varying and nonlinearity or even a complete lack of the knowledge of the system. A number of approaches were proposed to handle these systems, such as adaptive control, variable structure control, predictive control, robust control, and finally intelligent control. Adaptive control system can provide the ability to adjust operation parameters on-line according to input, output and state variables of the control system, which makes the controlled system have good control performance. But some complex systems with fast dynamic response, such as robot manipulators and high speed servo control system, are often found to suffer great difficulties in adaptive control, because the required time to implement adaptive algorithms is more than the sample theorem. Recently some different intelligent control methods have been presented in electro-hydraulic proportional position system (EHPPS). El-Ibiary Yehia presented "Theory Design and Application

of Expert Hydraulic Servos"<sup>[1]</sup>, Zhao Tienan presented "Theoretical and Experimental Analysis on Fuzzy control of a hydraulic position servo"<sup>[2]</sup>, and some good results have been obtained in these papers. According to the parameters varying and nonlinear in EHPPS, a new intelligent pole placement strategy with digital flow compensation (DFC) has been presented in this paper, and it has been realized by single chip microcomputer, which improves the control performance and simplifies the structure of the EHPPS. Since the system was successfully researched in 1993, it has been applying in the areas of machine tool, mechanical engineering etc.

## 2 SYSTEM STRUCTURE

### 2.1 The Model of the System

The EHPPS discussed in this paper is shown in Fig. 1. It consists of an unsymmetric hydraulic cylinder, four way symmetrically proportional valve, digital controller, PWM driving circuit, displacement and pressure sensors.

In EHPPS, the dynamic performance of the system mainly depends on the hydraulic natural frequency and damping ratio. Generally, the EHPPS can be expressed as three-order model

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shown in Fig. 2 under conditions of  $B_p k_{ce} / A_p^2 \ll 1$  and without spring load. The output displacement  $y(s)$  can be obtained as follows<sup>[5]</sup>:

$$y(s) = \frac{K_e \omega_h^2 R - (K_e / A^2) \times (1 + V_e / 4 \beta_e K_{tr}) W_h^2 F}{S^3 + 2 \zeta_h \omega_h S^2 + \omega_h^2 S + K_e \omega_h^2}$$

Because the hydraulic natural frequency, damping ratio and disturbance of the load are often varied in a wide range, which makes the dynamic response of the EHPPS be not easily satisfied, a new control strategy is needed to control EHPPS for improving its control performance.

## 2.2 Pressure Jumping

In our EHPPS, A single piston cylinder is used for simplifying the structure of the system. According to the results of reference[5], in the switching transient of symmetric four way valve controlling unsymmetric cylinder, large pressure jumping will occur, which makes flow discontinuity and unsteady moving of the system. In this paper, DFC is presented to overcome pressure jumping.

## 3 CONTROL STRATEGY

### 3.1 Pole Placement

In order to improve dynamic performance of EHPPS, a state feedback controller shown in Fig. 3 is used for pole placement, the eigen equation of closed-loop system can be obtained as follows:

$$S^3 + (K \cdot h_3 + 2 \cdot \zeta_h \cdot \omega_h) S^2 + (K \cdot h_2 + \omega_h^2) S + K \cdot h_1 = 0 \quad (2)$$

where  $K = K_v \cdot \omega_h^2$

Let the eigen equation be

$$[S^2 - (l_1 + \bar{l}_1) S + l_1 \cdot \bar{l}_1] (S + l_2) = 0 \quad (3)$$

where  $l_1, \bar{l}_1$  are a pair of conjugate complex roots,  $l_2$  is a real root.

It is preferable and more practical to place  $l_2$  far away from imaginary axis so that the eigen

equation has two predominant poles which are decided by the damping ratio and natural frequency of closed-loop system. Thus equation (3) can be expressed as follows:

$$S^3 + (l_2 + 2 \cdot \zeta_b \cdot \omega_b) S^2 + (2 \cdot \zeta_b \cdot \omega_b \cdot l_2 + \omega_b^2) S + \omega_b^2 \cdot l_2 = 0 \quad (4)$$

where  $\zeta_b, \omega_b$  are respectively damping ratio and natural frequency of the state feedback closed-loop system.

According to equations (2), (4), the feedback control parameters can be obtained as follows:

$$h_1 = l_2 \omega_b^2 / K$$

**Fig. 2 The simplified diagram of EHPPS**

**Fig. 3 The diagram of EHPPS with state feedback, intelligent parameter turning and digital flow compensation**

$$h_2 = (2 \cdot \zeta_b \cdot \omega_b \cdot l_2 + \omega_b^2 - \omega_h^2) / K$$

$$h_3 = (l_2 + 2 \cdot \zeta_b \cdot \omega_b - 2 \cdot \zeta_h \cdot \omega_h) / K$$

### 3. 2 Intelligent Parameter Turning (IPT)

The IPT is based on pattern recognition approach, the parameters ( $h_1, h_2, h_3$ ) are turned when parameters of the controlled system ( $\zeta_h, \omega_h$ ) are varied or a load disturbance occurs. The error signal between the set point and the displacement output of the EHPPS is monitored and compared with the desired peaks of error  $e_1, e_2, e_3$  as shown in Fig. 4.

Fig. 4 The step response

From equation (2), the action of  $h_1$  is the system gain,  $h_2$  increases frequency bandwidth of the controlled system, and  $h_3$  increases damping ratio of the controlled system. By making  $|e_1| \leq \sigma_1, |e_2| \leq \sigma_2, |e_3| \leq \sigma_3$ , and  $a_1 < t_r < a_2$ , we can turn  $h_1, h_2, h_3$  in its action. The knowledge of turning  $h_1, h_2, h_3$  is mainly used as follows:

- (1) If  $|e_1| < \sigma_1, |e_2| < \sigma_2, |e_3| < \sigma_3$  but  $t_r > a_2$ , then  $h_1$  and  $h_2$  should be increased,  $\Delta h_1 / \Delta h_2$  can be equal to a constant  $K_1$ .
- (2) If there is no overshoot, then  $h_1$  should be increased and  $h_3$  should be decreased,  $\Delta h_1 / \Delta h_3$  can be equal to a constant  $K_2$ .
- (3) If  $|e_1| > \sigma_1$ , then  $h_3$  should be increased and  $h_1$  should be decreased,  $\Delta h_3 / \Delta h_1$  can be equal to a constant  $K_3$ .
- (4) If  $|e_1| < \sigma_1, |e_2| > \sigma_2$ , then  $h_3$  should be increased.
- (5) If  $t_r < a_1$ , then  $h_1$  and  $h_2$  should be

decreased,  $\Delta h_1 / \Delta h_2$  can be equal to a constant  $K_4$ .

- (6)  $\Delta h_i / h_i$  is equal to 0.01,  $K_i$  is equal to 10,  $i = 1, 2, 3, 4$  respectively.

### 3. 3 Existential Theorem of Intelligent Parameter Adjusting

Suppose the controlled system is adjusted by using the parameters ( $h_1, h_2, h_3$ ) of closed-loop pole placement, and at the area of  $[h_1 + \Delta h_1, h_2 + \Delta h_2, h_3 + \Delta h_3]$ , respectively adjusting  $h_1, h_2, h_3$ , the system has steady and monotonic performance index  $J$ , and also  $J$  is continuous and differential for  $h_1, h_2, h_3$ , then a set of optimum parameters  $[h_1 + \Delta h_1^*, h_2 + \Delta h_2^*, h_3 + \Delta h_3^*]$  certainly exists, which makes the system have optimum performance index  $J^* [h_1 + \Delta h_1^*, h_2 + \Delta h_2^*, h_3 + \Delta h_3^*]$ , where optimum index can be

$$\min \int_0^t e^2 dt \text{ or } \min \int_0^t |e| t \times dt$$

and so on, which can be proved as follows.

$$\begin{aligned} \therefore J^* [h_1 + \Delta h_1^*, h_2 + \Delta h_2^*, h_3 + \Delta h_3^*] \\ = J[h_1, h_2, h_3] + OJ[h_1, h_2, h_3] \end{aligned}$$

According to the supposition, we get

$$J^* [h_1 + \Delta h_1^*, h_2, h_3] \leq J[h_1, h_2, h_3]$$

$$J^* [h_1, h_2 + \Delta h_2^*, h_3] \leq J[h_1, h_2, h_3]$$

$$J^* [h_1, h_2, h_3 + \Delta h_3^*] \leq J[h_1, h_2, h_3]$$

$$\therefore J^* [h_1 + \Delta h_1^*, h_2 + \Delta h_2^*, h_3 + \Delta h_3^*]$$

$$= J^* [h_1^*, h_2^*, h_3^*] < J[h_1, h_2, h_3]$$

where  $h_1^* = h_1 + \Delta h_1^*, h_2^* = h_2 + \Delta h_2^*, h_3^* = h_3 + \Delta h_3^*, [h_1^*, h_2^*, h_3^*]$  is optimum adjusting parameters, they can make index optimized.

### 3. 4 Digital Flow Compensation

In Fig. 1, the load flow of the four way proportional valve can be expressed as:

$$Q_{L1} = C_d W X_v \sqrt{(P_S - P_{L1}) / \rho} = K_1 I_1 \sqrt{P_S - P_{L1}} \tag{5}$$

$$Q_{L2} = C_d W X_v \sqrt{(P_S - P_{L2}) / \rho} = K_2 I_2 \sqrt{P_S - P_{L2}} \tag{6}$$

where  $K_1 = C_d W K_x \sqrt{1 / \rho}$

$$K_v = K_x I$$

let

$$I_1 = K_u U = K_u e \sqrt{DP_S / (P_S - P_{L1})}$$

$$e > 0 \tag{7}$$

$$I_2 = K_u U = K_u e \sqrt{DP_S / (P_S - P_{L2})}$$

$$e > 0 \tag{8}$$

where  $D$  is a constant which can be selected between 0.5 to 1. From equation (6) to (9), we get  $Q_L = Q_{L1} = Q_{L2} = K_1 K_u e (DP_S)^{1/2}$  therefore, after DFC, the load flow is only proportional to error voltage, and it is not affected by load pressure. The value of parameter  $D$  influences the flow gain, it should be adjusted in the actual application.

## 4 SIMULATION AND EXPERIMENT RESULTS

### 4.1 Simulation Results

Considering the EHPPS shown in Fig. 1, let the parameters of the controlled system be  $\zeta_h = 0.2$ ,  $\omega_h = 26$ ,  $k = 400$ ; and selecting the parameters of the state feedback closed-loop control system  $\zeta_b = 0.7$ ,  $\omega_b = 30$ ,  $l_2 = 10$ , the simulation result of tracking a square wave reference signal is shown in Fig. 5. The step response of parameter varying is given in Fig. 6, curve 1 shows  $\zeta_h = 0.2$  varying to  $\zeta_h = 0.4$ , curve 2 shows  $\omega_h = 26$  varying to  $\omega_h = 20$ , curve 3 shows  $k = 400$  varying to  $k = 300$ . It is clearly seen that the control strategy presented in the paper not only possesses better response performance but also has much better robustness with response to the system's parameter varying.

### 4.2 Experiment Results

The dynamic performance of the experiment equipment for tracking a sine wave reference signal is shown in Fig. 7, and step response of the displacement output is shown in Fig. 8. Satisfactory dynamic and steady characteristics can be seen in Fig. 7 and Fig. 8.

## 5 CONCLUSIONS

(1) The pole placement control method

associated with intelligent parameters adjusting can obtain good dynamics and steady response of the EHPPS, this control strategy can be used at other servo control system.

(2) The algorithm of intelligent parameter adjusting is convergence for monotonic and diff-

Fig. 5 Square-wave response

Fig. 6 The step response with parameters varying

Fig. 7 The sine wave response of EHPPS

### Fig. 8 The step response of EHPPS

erential system, but it should be further researched for speeding up its speed of convergence.

(3) DFC is a digital nonlinear compensation method, it can overcome flow jumping which is caused by pressure jumping, and improve the positioning precision of the EHPPS.

(4) Intelligent parameter adjusting approach takes less time than adaptive control method, and can be easily realized by single chip processor, thus results in the reduction of the system hardware and cost. Therefore it can be applied in industrial fields.

### Nomenclature

$P_s$ : supply pressure  
 $K_v$ : flow gain of the valve  
 $\omega_h$ : natural frequency of the system  
 $\xi_h$ : damping ratio of the system  
 $K_{ce}$ : total leakage coefficient  
 $A$ : effective area of the cylinder piston  
 $V_t$ : the volume of the cylinder  
 $\beta_e$ : equivalent bulk modulus elasticity  
 $F$ : external disturbance force

$R$ : displacement input signal  
 $Y$ : displacement output of the EHPPS  
 $P_{L1}$ : load pressure at one port  
 $P_{L2}$ : load pressure at other port  
 $\delta_1, \delta_2, \delta_3, a_1, a_2, D$ : positive constant  
 $t_r$ : rising time of the system  
 $e$ : the error between input and output  
 $\omega_b$ : natural frequency of the closed-loop system  
 $\xi_b$ : damping ratio of the closed-loop system  
 $l_2$ : the pole of closed-loop system which is far away from the imaginary axis  
 $K$ : the closed-loop gain  
 $h_1, h_2, h_3$ : the state feedback parameters  
 $K_u$ :  $K_u = I/U$ ,  $U$  is voltage of providing to proportional valve,  $I$  is current of providing to proportional valve  
 $X_v$ : the valve spool movement of the proportional valve  
 $Q_{L1}$ : load flow at one port  
 $Q_{L2}$ : load flow at other port  
 $W$ : port width of the valve  
 $C_d$ : flow coefficient  
 $\rho$ : density of the working fluid

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